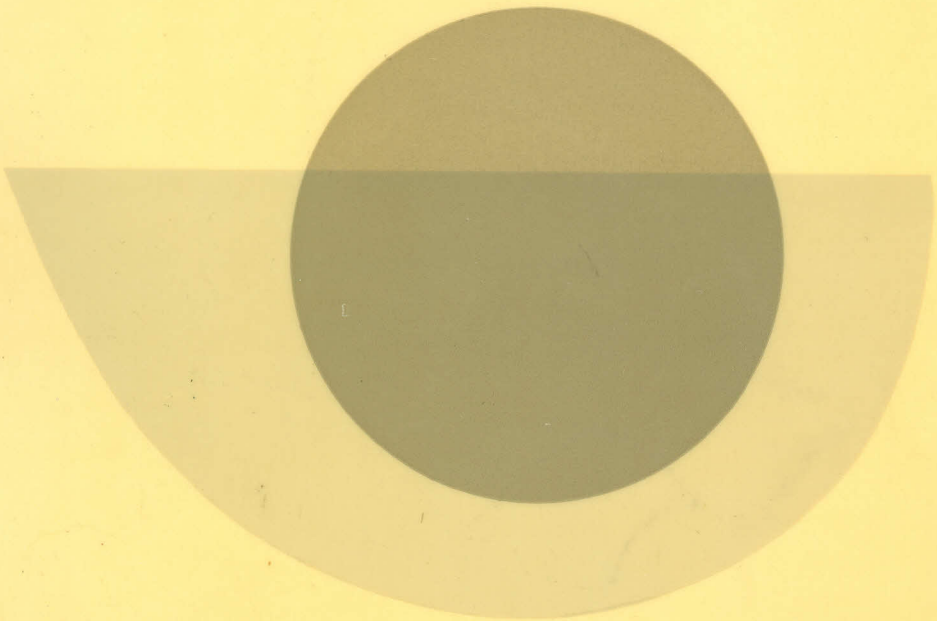
Geophysics and Astrophysics Monographs

Atmospheric Thermodynamics

J. V. Iribarne and W. L. Godson



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ATMOSPHERIC THERMODYNAMICS

by

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